Reg.No.....

Name.....

### APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

FIRST SEMESTER B.TECH DEGREE (SUPPLEMENTARY) EXAMINATION, FEBRUARY 2017 (2015 ADMISSION)

Course Code: MA 101 Course Name: CALCULUS

Max.Marks: 100

Duration: 3 Hours

#### PART A

(Answer all questions. Each question carries 3 marks)

1) Show that the series  $\sum_{n=1}^{\alpha} \left(\frac{1}{2}\right)^n$  converges.

2) Classify the surface  $z = (x - 1)^2 + (y + 2)^2 + 3$ 

3) Find the Maclaurin series for cos x

4) Evaluate  $Lt_{(x,y)\to(-1,2)} \frac{xy}{x^2+y^2}$ 

5) Convert the cylindrical co-ordinate into rectangular co-ordinate of  $(4, \pi/3 - 3)$ .

6) Find the slope of the surface  $z = xy^2$  in the x direction at the point (2,3).

7) Find the directional derivative of  $f = x^2y - yz^3 + z$  at (1,-2,0) in the direction of  $\vec{a} = 2\vec{i} + \vec{j} + 2\vec{k}$ 

8) Find the unit normal to the surface xy + xz + yz = c at (-1,2,3)

9) Evaluate  $\iint_{1}^{ab} x^2 y \, dx dy$ 

10) Find the area of the region R enclosed by y=1, y=2, x=0, x=y .

#### PART B

(Answer any 2 questions. Each question carries 7 marks)

11) Test the absolute convergence of  $\sum_{n=1}^{\alpha} \frac{(-1)^n n^4}{4^n}$ 

12) Determine the Taylor's series expansion of  $f(x) = \sin x$  at  $x = \pi/2$ .

13) Test the convergence of  $\frac{1}{1.2.3} + \frac{3}{2.3.4} + \frac{5}{3.4.5}$ .....

## (Answer any 2 questions. Each question carries 7 marks)

- 14) Find the equation of the paraboloid  $z = x^2 + y^2$  in the cylindrical and spherical coordinates.
- 15) Find F(f(x),g(y),h(z)) if  $F(x,y,z) = y e^{xyz}$ ,  $f(x) = x^2$ , g(y) = y + 1,  $h(z) = 2z^2$
- 16) By converting into polar coordinate evaluate  $\lim_{(x,y)\to(0,0)} \sqrt{x^2+y^2} \ln\left(\left(x^2+y^2\right)^2\right)$

## (Answer any 2 questions. Each question carries 7 marks)

- 17) Find the local linear approximation L of f(x,y,z) = xyz at the point P(1,2,3). Compare the error in approximating f by L at the point Q(1.001, 2.002, 3.003) with the distance PQ.
- 18) Find the relative extrema of  $f(x, y) = 3x^2 2xy + y^2 8y$
- 19) If f is a differentiable function of three variables and suppose that

$$w = f(x - y, y - z, z - x)$$
 Show that  $\frac{\partial w}{\partial x} + \frac{\partial w}{\partial y} + \frac{\partial w}{\partial z} = 0$ 
Answer any 2 questions. Each question carries 7 marks)

20) Suppose that a particle moves along a curve in 3-space so that its position vector at time t is  $r(t) = 4\cos \pi t i + 4\sin \pi t j + t k$ . Find the distance travelled and the displacement of the particle during the time interval  $1 \le t \le 5$ 

- 21) A particle is moving along the curve,  $\vec{r} = (t^3 2t)\vec{i} + (t^2 4)\vec{j}$  where t denotes the time. Find the scalar tangential and normal components of acceleration at t = 1. Also find the vector tangential and normal components of acceleration at t = 0.
- 22) Find the arc length of the parametric curve  $x = 5\cos t$ ,  $y = 5\sin t$ , z = 2t;  $0 \le t \le \pi$

# (Answer any 2 questions. Each question carries 7 marks)

- 23) Evaluate the integral by converting into polar co ordinates  $\int_{0}^{2\sqrt{4-x^2}} \int_{0}^{2} (x^2 + y^2) \, dy \, dx$
- 24) Using triple integral to find the volume bounded by the cylinder

$$x^2 + y^2 = 4$$
 and the planes  $z = 0$  and  $y + z = 3$ 

25) Change the order of integration and evaluate  $\iint_{0}^{1} \frac{x}{x^2 + y^2} dx dy$ 



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