Reg. No.:	
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Name:			

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

FIRST SEMESTER B.TECH DEGREE SPECIAL EXAMINATION, AUGUST 2016

Course Code: MA101

Course Name: CALCULUS

Max. Marks: 100

Duration: 3 Hours

PART A

Answer ALL questions. Each question carries 3 marks

- Find derivative of y = sinh (4x-8)
- 2. Test whether the series converges or diverges, $\sum_{k=1}^{\infty} \frac{k}{2^k}$
- 3. Identify the surface $z = y^2 x^2$
- Convert from rectangular to spherical co-ordinates, (2√3, 2, -4)
- 5. Find $\frac{\partial Z}{\partial x}$ and $\frac{\partial Z}{\partial y}$ if $Z = \cos(xy^3)$
- 6. Show that \$\frac{\partial^2 z}{\partial x \partial y} = \frac{\partial^2 z}{\partial y \partial x}\$ if \$z = x^2 y + 5 y^3\$.
 7. Evaluate \$\int_0^2 (2t\hat{t} + 3t^2) dt\$
 8. Find the arc length of the parametric curve \$x = e^t\$, \$y = e^t\$ \$, \$z = \sqrt{2} t\$ \$, \$0 \leq t \leq 1\$.
 9. Evaluate \$\int_0^3 \int_0^4 \int_0^2 \quad \text{5} \text{2} \quad \text{5} \text{2} \quad \text{5} \quad \text{5}\$.

- 9. Evaluate $\int_{1}^{3} \int_{2}^{4} (40 20 \ xy) \ dy \ dx$
- 10. Evaluate $\int_0^3 \int_0^2 \int_0^1 (xyz) dx dy dz$

PART B

Answer any 2 complete questions each having 7 marks

- 11. Test the convergence of the series $\sum\nolimits_{k=1}^{\infty} \frac{k(k+3)}{(k+1)(k+2)(k+5)}$
- 12. Show that $\sinh^{-1} x = \ln\left(x + \sqrt{x^2 + 1}\right)$
- 13. Find the Taylor series of $\frac{1}{x+2}$ about x=1.

Answer any 2 complete questions each having 7 marks

14. Express the equation $x^2 - y^2 - z^2 = 0$ in cylindrical and spherical coordinates.

- $(\sqrt{x^2 + y^2})]/(x^2 + y^2)$ by converting to polar coordinates. 15. Evaluate $\lim_{(x,y)\to(0,0)}$ [sin
- 16. Show that the functions $f(x, y) = 3x^2y^5$ and $f(x, y) = \sin(3x^2y^5)$ are continuous everywhere.

Answer any 2 complete questions each having 7 marks

- 17. Let L(x, y) denote the local linear approximation to $f(x, y) = \sqrt{x^2 + y^2}$ at the point (3, 4). Compare the error in approximating f (3.04, 3.98) = $\sqrt{(3.04)^2 + (3.98)^2}$ by L (3.04, 3.98) with the distance between the points (3,4) and (3.04, 3.98).
- 18. Suppose that $w = x^2 + y^2 z^2$ and $x = \rho \sin \phi \cos \theta$, $y = \rho \sin \phi \sin \theta$, $z = \rho \cos \phi$. appropriate form of the chain rule to find $\frac{\partial w}{\partial a}$ and $\frac{\partial w}{\partial \theta}$
- 19. Locate the relative extrema and saddle points of $f(x, y) = 3x^2 2xy + y^2 8y$

Answer any 2 complete questions each having 7 marks

- 20. Let $f(x, y) = x^2 e^y$. Find the maximum value of a directional derivative at (-2,0) and find the
- unit vector in the direction in which the maximum value occur.

 21. Find the angle between the tangent lines to the graphs of $t_i(t) = \tan^{-1} t \, i + \sin t \, j + t^2 \, k$ $r_2(t) = (t^2 - t)i + (2t - 2)j + \log t$
- 22. Suppose that a particle moves through 3-space so that its position vector at time t is $r(t) = ti + t^2 i + t^3 k$.

Find the scalar tangential and normal components of acceleration at time t = 1.

Answer any 2 complete questions each having 7 marks

- 23. Use a polar double integral to find the area enclosed by the circle $r = sin\theta$
- 24. Use a triple integral to find the volume of the solid within the cylinder $x^2 + y^2 = 9$ and between the planes z = 1 and z = 5
- 25. Evaluate $\iint_{a} \frac{x-y}{x+y} dA$ where R is the region enclosed by x-y=0, x-y=1, x+y=1, x + y = 3